Converting Between Decimal form and DMS Form

This example is taken from page 414 in your textbook.

Minutes and Seconds

Fractional parts of a degree are usually expressed in decimal form or in *minutes* and *seconds*. A **minute** (') is $\frac{1}{60}$ of a degree, and a **second** ('') is $\frac{1}{3600}$ of a degree. This form is often called **DMS Form**, for degrees, minutes, and seconds.

Example:

(a) Write $35^{\circ} 15' 27''$ in decimal form.

$$35^{\circ} \ 15' \ 27'' = 35^{\circ} + \left(\frac{15}{60}\right)^{\circ} + \left(\frac{27}{3600}\right)^{\circ}$$
$$= 35^{\circ} + 0.25^{\circ} + 0.0075^{\circ}$$
$$= 35.2575^{\circ}$$

(b) Write 48.3625° in DMS form.

First, convert the entire decimal part to minutes by writing it in terms of $\frac{1}{60}$ of a degree.

$$48.3625^{\circ} = 48^{\circ} + 0.3625^{\circ} = 48^{\circ} + \left(\frac{60}{60}\right) 0.3625^{\circ}$$
$$= 48^{\circ} + \left(\frac{21.75}{60}\right)^{\circ} = 48^{\circ} + 21.75'$$

Second, convert the decimal part of the mins to seconds by writing it in terms of $\frac{1}{60}$ of a minute.

$$48^{\circ} + 21.75' = 48^{\circ} + 21' + \left(\frac{60}{60}\right) 0.75'$$
$$= 48^{\circ} + 21' + \left(\frac{45}{60}\right)'$$
$$= 48^{\circ} 21' 45''$$

Convert the following two angles:

- 1. 87° 15′ 36″
- 2. -17.6243°

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